## EXERCISES S-38.215: WEEK 5

## Exercise 12:

Consider the fluid model for the TCP source described in the lecture of this week. Assume that the TCP source can only be in two states  $(S = \{1,2\})$  and that r < c < 2r. Show that

$$F_{1}(y) = F_{1}(K) \cdot e^{\theta(y-K)},$$
  

$$F_{2}(y) = F_{1}(K) \cdot \frac{c-r}{2r-c} \left[ e^{\theta(y-K)} - e^{-\theta K} \right],$$

where  $\theta = \lambda/(c-r)$  and

$$F_1(K) = \frac{\mu}{\lambda + \mu} \left[ 1 + \frac{\mu}{\lambda + \mu} \frac{c - r}{2r - c} (1 - e^{-\theta K}) \right]^{-1}$$

Furthermore, show that the fraction of time that the buffer is congested is given by  $\lambda F_1(K)/\mu$ .

## Exercise 13:

Consider the basic fluid queue model with inflow regulated by an on-off source. Discuss what the effect on the buffer content is if the on-periods are given by

- a sum of a regularly varying period with index  $-\nu_1$  and a regularly varying period with index  $-\nu_2$ ;
- a mixture of a regularly varying period with index  $-\nu_1$  and a regularly varying period with index  $-\nu_2$  (i.e. a fraction of the on-periods is regularly varying with index  $-\nu_1$  and the remainder of the on-periods is regularly varying with index  $-\nu_2$ ).